



Teaching Math Classically with Andrew Elizalde

Lesson 15: Teaching Math as Storytelling

Outline:

According to David Hicks in *Norms and Nobility*, the difference between mytho-poetic pedagogy and an analytical pedagogy challenges us to consider the stories behind the concepts and introducing ideas through stories.

- International studies (particularly in Japan) show effectiveness and cohesion of the storytelling teaching style.
- How often are our lessons interrupted from beginning to end with (for example) announcements, abrupt steps from one section of the lesson to the next?
- How can we connect all ideas through a narrative?
- According to James Stigler and James Hiebert in *The Teaching Gap*, Japanese storytelling lessons are treated as “sacred,” planned as “complete experiences” with a beginning, a middle, and an end.
 - The meaning is in the connection between the parts.
- In Kieran Egan’s *Teaching as Story Telling: An Alternative Approach to Teaching and Curriculum in Elementary School*, storytelling needs to become part of our pedagogy.
 - Our teaching is often “inappropriately mechanistic.”
 - We underuse our students’ imaginations.
 - We should think in terms of stories to be told rather than objectives reached.
 - Math can be “rehumanized” by tying computational tasks back to the human reason people began to do them in the first place.
 - What is the history of how people began to use this concept?

How can math teachers be good storytellers?

- A good story has:
 - Tension to be resolved (solving a difficult problem)
 - Rhythm (tension to resolution, then repeat the cycle)
 - Beginning, middle, and an end
 - Plato’s *Phaedrus*
 - Aristotle
 - George Kennedy: *Classical Rhetoric and Its Christian and Secular Tradition*



Early History of Trigonometry

Whiteboard exercise (time stamp 9:38)

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$$\sin \Theta = \frac{\text{opp}}{\text{hyp}}$$

$$\sin 30^\circ = \frac{1}{2}$$

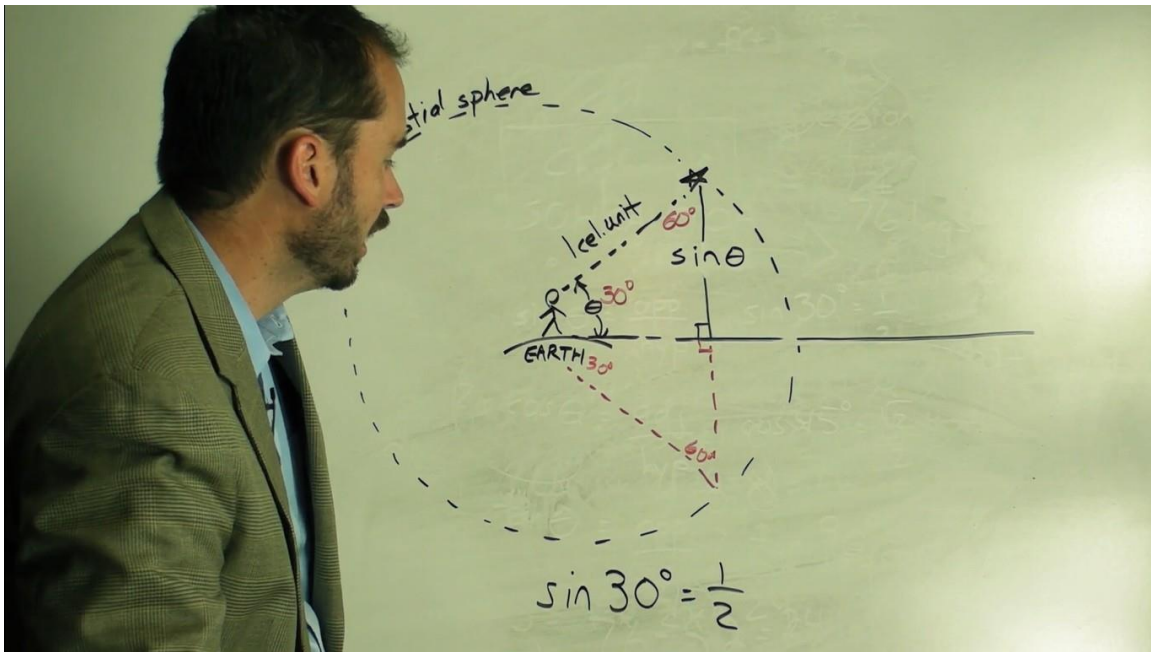
$$\cos \Theta = \frac{\text{adj}}{\text{hyp}}$$

$$\cos 45^\circ = \frac{\sqrt{2}}{2}$$

$$\tan \Theta = \frac{\text{opp}}{\text{adj}}$$

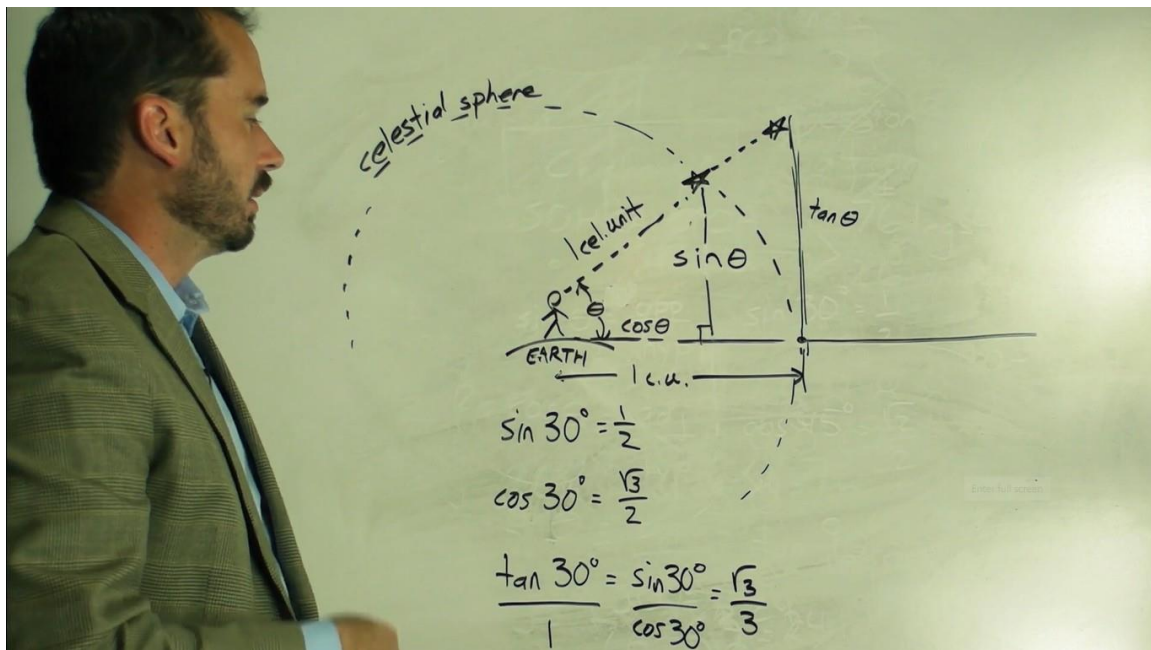
$$\tan 90^\circ = \emptyset \quad (11:28)$$

- But where is the context for these ideas? What is the history of this concept?
- Let's say you are a twelfth-century astronomer. It's night and you're looking at the sky. You see the stars there. You realize the stars "shift" or rotate. The earth (at the center, of course) has a celestial sphere around it. (14:10)
 - How far away are the stars from the earth? The distance can be called a "celestial unit." (15:00)
- Orientation is defined by distance from me to horizon to star the distance above the point on the horizon = sine. (16:50)
- Sine depends on the angle you look at the star from. If the angle is θ , and the distance is sine of θ or $\sin \theta$. (18:24)
 - If the θ angle is 30° , then we can figure the other angles. (18:56) The segments extended form an equilateral triangle. (19:48)
- Half of the celestial unit = $\sin \theta$ $\sin 30^\circ = \frac{1}{2}$



- We can figure 45° and 60° from the same illustration.
- The story continues for students the next day with other portions of the triangle... cosine or $\cos \theta$.
- With a further star, the “shadow length” $\tan \theta$ (23:00).
- $\sin 30^\circ = \frac{1}{2}$ $\cos 30^\circ = \frac{\sqrt{3}}{2}$
- The distance from the viewer to the edge of the horizon is also 1 celestial unit. Look for similar triangles—the ratio of corresponding sides is constant. Therefore:

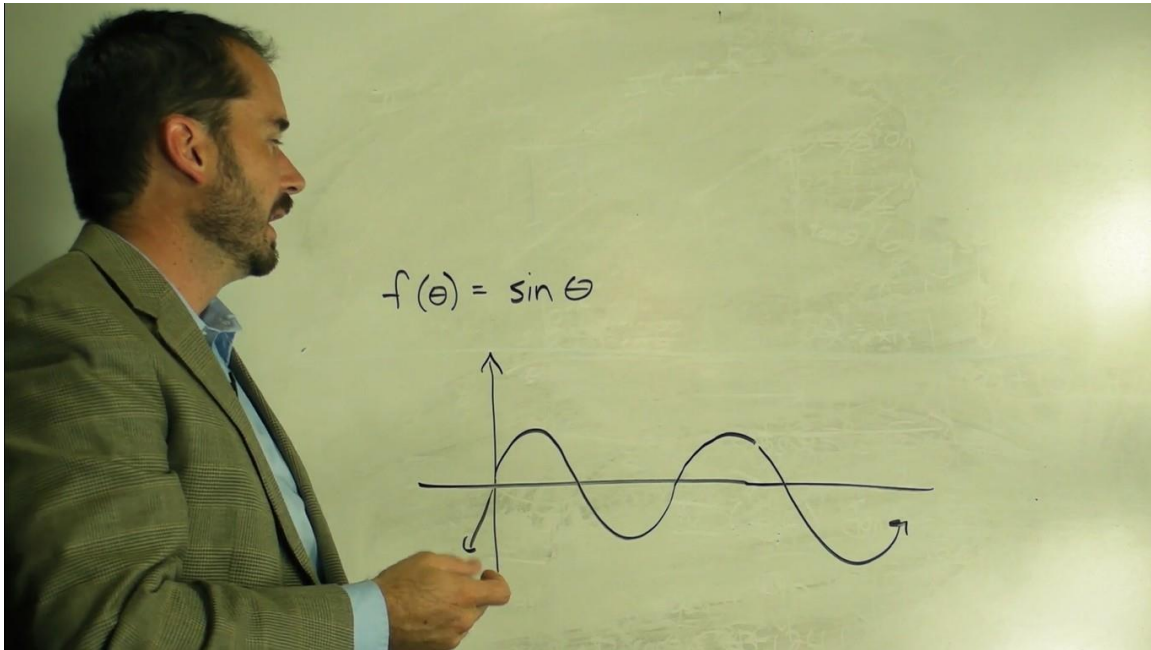
$$\frac{\tan 30^\circ}{1} = \frac{\sin 30^\circ}{\cos 30^\circ} = \frac{\sqrt{3}}{3}$$



- The teacher can use the same picture this whole time.
- Building a new idea, but coming back to the same picture. This is the poetic rhythm of building the story.
- What if there's an even further star?
 - The hypotenuse of the new triangle
 - The side adjacent the angle = adjacent
 - The side opposite the angle = opposite (28:30)
 - Using ratios, we get...

$$\begin{array}{ccccc}
 \sin \theta & = & \text{opp} & \cos \theta = \text{adj} & \tan \theta = \text{opp} \quad (30:50) \\
 1 \text{ c. unit} & & \text{hyp} & 1 \text{ c} & \text{hyp} \quad 1 \text{ cu} \quad \text{adj}
 \end{array}$$

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- This creates models for natural phenomena that we still use today, as in representations of music.
- These stories are not found in textbooks, so teachers are required to know the history and synthesize it for the students.

Challenge: Is there one concept whose history might be investigated? Could you experiment with bringing that history into your math classroom?